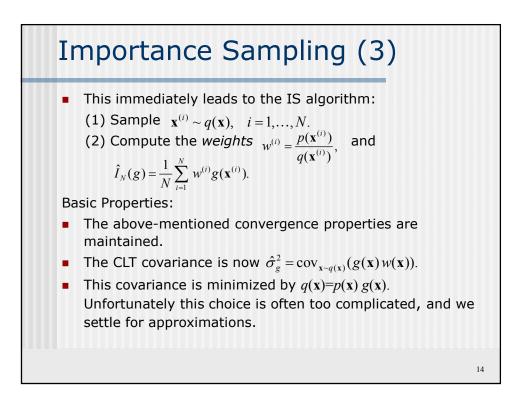
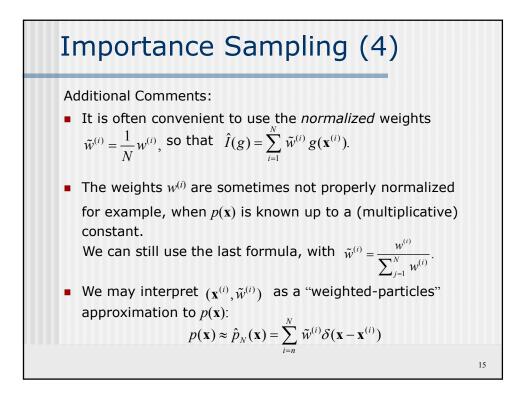
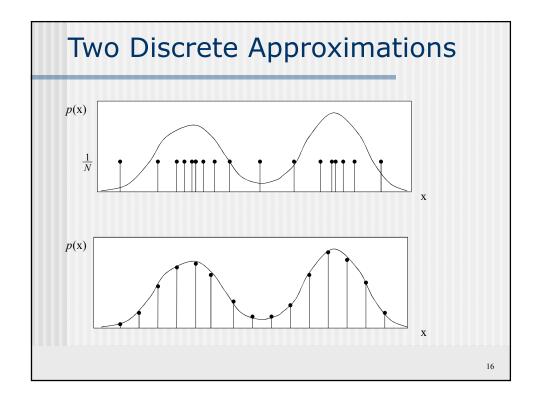
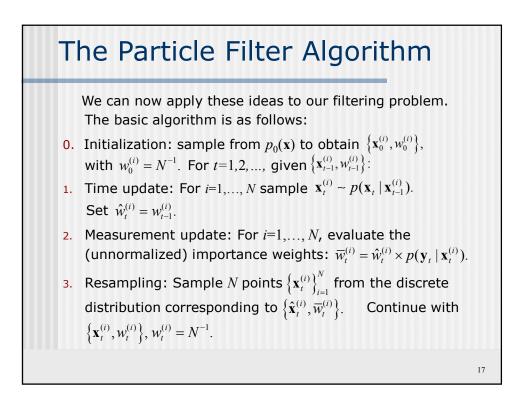


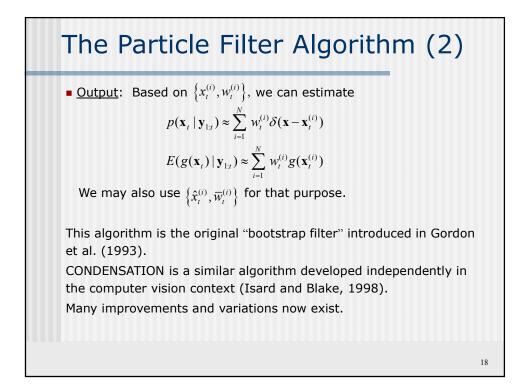
<section-header>**DESCRIPTION**
 Sumportance Sampling (2)• Let $q(\mathbf{x})$ be a selected distribution over \mathbf{x} - the
 proposal distribution. Assume that $p(\mathbf{x}) < 0 \Rightarrow q(\mathbf{x}) < 0$.• Observe that: $I(g) = \int g(\mathbf{x}) p(\mathbf{x}) d\mathbf{x} = \int g(\mathbf{x}) \frac{p(\mathbf{x})}{q(\mathbf{x})} q(\mathbf{x}) d\mathbf{x}$
 $= \int g(\mathbf{x}) w(\mathbf{x}) q(\mathbf{x}) d\mathbf{x}$ where $w(\mathbf{x}) = \frac{p(\mathbf{x})}{q(\mathbf{x})}$ is the likelihood ratio, or simply the weight-function.

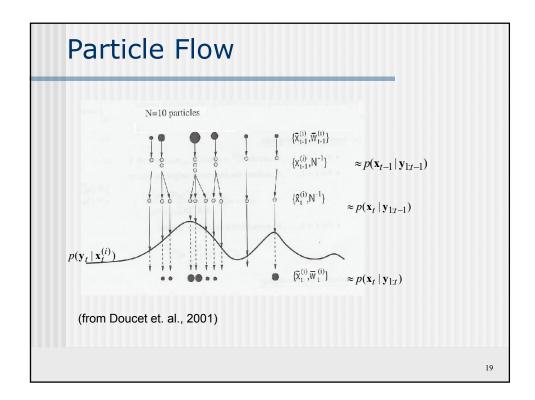


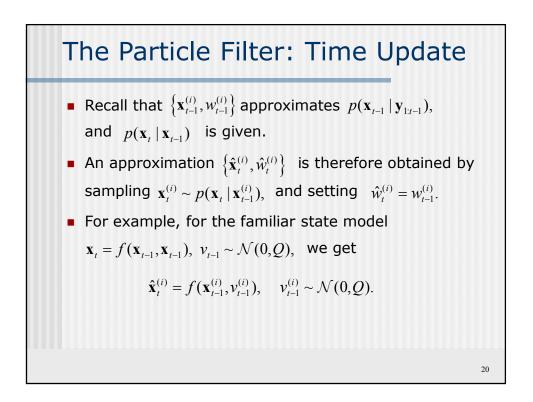


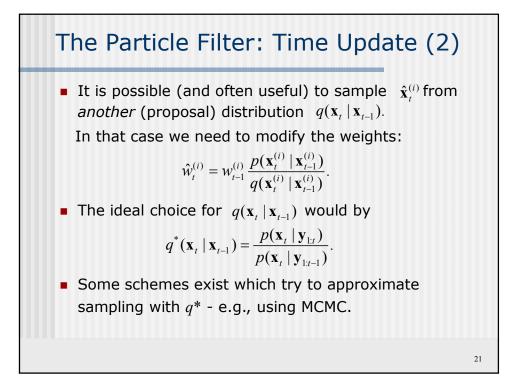




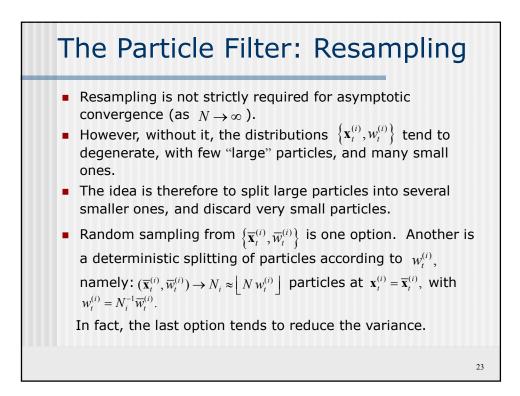


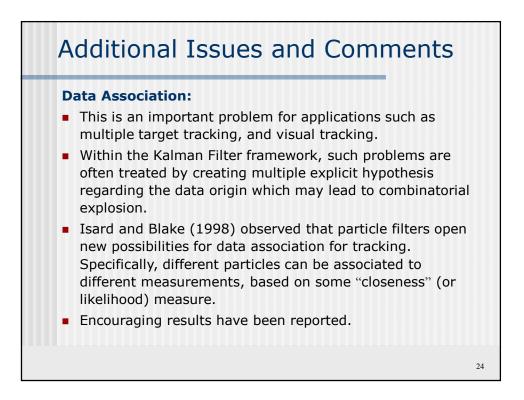


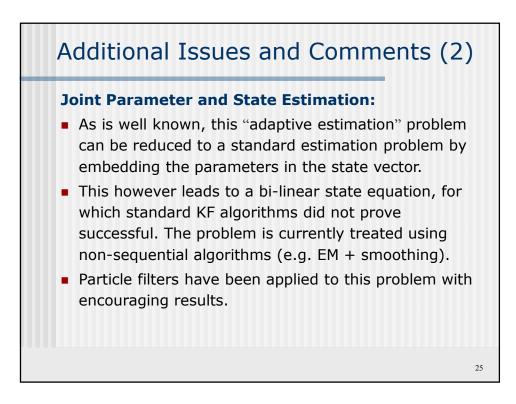


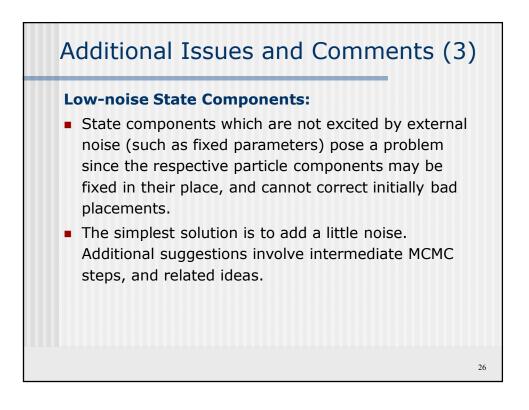


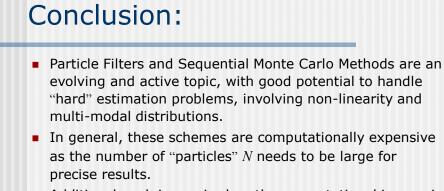
The Particle Filter: Measurement Update • Recall that $p(\mathbf{x}_t | \mathbf{y}_{1:t}) = \frac{1}{c} p(\mathbf{y}_t | \mathbf{x}_t) p(\mathbf{x}_t | \mathbf{y}_{1:t-1}),$ and $\{\hat{\mathbf{x}}_t^{(i)}, \hat{w}_t^{(i)}\}$ approximate $p(x_t | y_{1:t-1}).$ • To obtain an approximation $\{\overline{\mathbf{x}}_t^{(i)}, \overline{w}_t^{(i)}\}_{t=1}^N$ to $p(\mathbf{x}_t | \mathbf{y}_{1:t}),$ we only need to modify the weights accordingly: $\overline{w}_t^{(i)} = \hat{w}_t^{(i)} p(\mathbf{y}_t | \hat{\mathbf{x}}_t^{(i)}),$ with $\overline{\mathbf{x}}_t^{(i)} = \hat{\mathbf{x}}_t^{(i)}.$











- Additional work is required on the computational issue in particular, optimizing the choice of *N*, and related error bounds.
- Another promising direction is the merging of sampling methods with more disciplined approaches (such as Gaussian filters, and the Rao-Blackwellization scheme ...).

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