TECHNION - ISRAEL INSTITUTE OF TECHNOLOGY

FACULTY OF MATHEMATICS

Handout 1	
General Information	

Winter 2023–24 Igal Sason

Selected Topics in Information Theory and Combinatorics (106717)

Instructor: Prof. Igal Sason (office: Meyer 652, e-mail: sason@ee.technion.ac.il).

Time and Place: Tuesdays 10:30-12:30 (Ullman 705) and 14:30-15:30 (Ullman 102).

Credit Points: 3.0 academic points. A joint undergraduate-graduate course.

Prerequisites: Elementary (undergraduate) courses in calculus, combinatorics, linear algebra, and probability. *No prior knowledge in information theory is assumed.*

Language: Hebrew, unless there will be demand to give it in English.

Grading Policy: Semester exams: Final A (07.05.2024), and Final B (04.06.2024). Homework assignments are not for submission but are very recommended (also for the final exams).

Course outline (Tentative) [3 hours per week, 12 weeks - 36 hours]:

- 1. Shannon entropy, (conditional) mutual information, divergences and f-divergences (5 hours).
- 2. Han's inequality and Shearer's lemma. A combinatorial application (1 hour).
- 3. Channels, data-processing inequalities, chain rules, and convexity properties (3 hours).
- 4. AEP, and almost lossless compression for discrete memoryless sources (3 hours).
- 5. Differential entropy and applications in matrix theory (3 hours).
- 6. Information theory and problems in extremal combinatorics (6 hours).
- 7. Method of types, universal compression, Sanov's theorem (5 hours).
- 8. Submodularity, information inequalities, and combinatorial applications (4 hours).
- 9. Entropy rates of discrete-time stationary processes (1 hour).
- 10. Shannon capacity of graphs for zero-error communication (5 hours).

References

- [1] M. Aigner and G. M. Ziegler, *Proofs from the Book*, Springer, 6th edition, 2018.
- [2] T. M. Cover and J. A. Thomas, *Elements of Information Theory: Second Edition*, 2006.
- [3] S. Jukna, *Extremal Combinatorics with Applications in Computer Science*, 2nd Edition, Springer, 2011.