

**Electrical Engineering Department** Computers **Communications** 





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lode 4 (8 x 10 thinned)

SNR = -15 dB

# **Cognitive Sub-Nyquist Collocated MIMO Radar Prototype**

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Main Contributions	<b>Conventional Collocated MIMO</b>	Sub-Nyquist MIMO	Signal Model and Recovery			
<ul> <li>Prototype realizes both spatial and temporal sub-Nyquist sampling in a MIMO radar without loss of angular and range resolution</li> </ul>	MIMO array with fewer elements has same spatial resolution as a virtual array with	<ul> <li>Spatial Sub-Nyquist         <ul> <li>Less antenna elements (randomly thinned arrays)</li> <li>Same angular resolution as of virtual array</li> </ul> </li> <li>Temporal Sub-Nyquist</li> </ul>	• Received signal for P pulses at the <i>q</i> th antenna after demodulation: Total number of Targets $trace = \sum_{p=0}^{P-1} \sum_{m=0}^{M-1} \sum_{l=1}^{L} \alpha_l h_m (t - \tau_l - p\tau) e^{j2\pi\beta_{m,q}\theta_l} e^{j2\pi f_l^D p\tau}$ $Target time delay$			

- Sub-Nyquist 4x5 MIMO array shows same detection performance as Nyquist 8x10 ULA
- Cognitive transmission is employed to further enhance SNR for sub-Nyquist arrays

more elements	$TR\frac{\lambda}{2}$ Virtual array	<ul> <li>Temporal Sub-Nyquist</li> <li>Reduced sampling rate at each Rx</li> </ul>	Composite Rx signal spectrum	•	Fourier coefficients of the $m$ th transmitter channel at the $q$ th receiver: Operating frequency
MIMO transmits orthogonal	Radar cross-section is same for all antennas in collocated MIMO	• Same range resolution as that of Nyquist bandwidth $TB_h$			$y_{m,q}^{p}[k] = \sum_{l=1}^{L} \alpha_{l} e^{j2\pi\beta_{m,q}\theta_{l}} e^{-j\frac{2\pi}{\tau}k\tau_{l}} e^{-j2\pi f_{m}\tau_{l}} e^{j2\pi f_{l}^{D}p\tau}$ Target reflectivity Dopplor focusing for a specific frequency y
waveforms and processes linear combination of		<ul> <li>Cognitive Transmission</li> <li>Entire power is focused in only few narrow subbands</li> </ul>	Nyquist MIMO Tx Waveform		$Doppier focusing for a specific frequency v$ $\phi_{m,q}^{v}[k] = \sum_{l=1}^{L} \alpha_{l} e^{j2\pi\beta_{m,q}\theta_{l}} e^{-j\frac{2\pi}{\tau}(k+f_{m}\tau)\tau_{l}} \times \begin{cases} P &  f_{l}^{D}-\nu  < 1/2P\tau \\ 0 & else \end{cases}$
to each waveform	R receivers T transmitters	• High SNR at receiver	Jub-Nyquist MIMO Tx Waveform	•	Recover azimuth, delay and Doppler using simultaneous sparse 3D OMP with focusing

## **Technical Specifications**

BW per Tx (incl. guard- bands) BW per Tx (excl. guard- bands) Temporal sampling rate Spatial sampling rate	Nyquist (Mode 1)15 MHz12 MHz30 MHz8x1080	Sub-Nyquist (Mode 3)3 MHz3 MHz3 MHz7.5 MHz4x520	Reduction         80%         75%         75%         50%         25%	Laptop/PC User Interface $s_r[n] = l_r[n] + jQ_r[n]$ Modes 1, 2 and 4 Mode 3 $T = 2^{20} MHz$ $T = 2^{20} MH$	Litter full spectrum of one channel of one receiver before subsampling at 7.5 MHz
	Array	Modes		Waveform Generator	Analog Pre-Processor (APP) Digital Receiver
Mode 1: Filled unifor Mode 2: Filled rand Mode 3 Thinned ran (~Virtual 8 Spatial sub Mode 4: Thinned ran (~Virtual 20	: 8x10 orm array : 8x10 om array 3: 4x5 dom array x10 ULA) o-Nyquist : 8x10 dom array x20 ULA)	$\begin{array}{c} \times \ Tx \\ \end{array} \\ \end{array} \\ \end{array} \\ \times \ \infty \\ \end{array} \\ \times \ \infty \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \times \ 0 \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} $ \\ \end{array}  \\ \end{array} \\ \end{array}		<ul> <li>Total BW, 8 Tx: 120 MHz 3 MHz guard-bands</li> <li>Eight 375 kHz cognitive slices per Tx</li> <li>Cognitive BW, 1 Tx: 3 MHz (= 8 x 375 kHz)</li> <li>BW reduction, 1 Tx (excl. guard-bands): 75% (3 of 12 Mhz)</li> <li>Kilinx VC707 FPGA Board</li> <li>Vilinx VC707 FPGA Board</li> <li>Vilinx</li></ul>	<ul> <li>APP filters the receiver data into eight channels</li> <li>Dual back-to-back APPs in a single chassis</li> <li>BPFs have ~30 dB stopband attenuation to mitigate subsampling noise</li> <li>BPFs have ~30 dB stopband attenuation to mitigate subsampling noise</li> <li>Two 16-bit eight, channel digitizers for I and Q streams</li> <li>Sub-Nyquist sampling rate: 7.5 MHz/channel</li> <li>Signal BW with guard-bands: 30 MHz/channel</li> </ul>

## **Overview of Hardware Architecture**



#### **User Interface \ Radar Display**

#### **Sample Measurements Results**



