Airborne Three-Dimensional Cloud Tomography

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Abstract

We seek to sense the three dimensional (3D) volumetric distribution of scatterers in a heterogenous medium. An important case study for such a medium is the atmosphere. Atmospheric contents and their role in Earth's radiation balance have significant uncertainties with regards to scattering components: aerosols and clouds. Clouds, made of water droplets, also lead to local effects as precipitation and shadows. Our sensing approach is computational tomography using passive multi-angular imagery. For light-matter interaction that accounts for multiple-scattering, we use the 3D radiative transfer equation as a forward model. Volumetric recovery by inverting this model suffers from a computational bottleneck on large scales, which include many unknowns. Steps taken make this tomography tractable, without approximating the scattering order or angle range.

1. Introduction

Scattering and refractive media are increasingly considered in computer vision [19, 20, 38, 39, 46, 48], typically for observing background objects [47, 35, 56]. However, in important cases, the medium itself is of interest. For example, remote sensing of the atmosphere seeks to assess the distribution of various airborne scatterers. Image data is used to fit a physical model of light propagation through the medium and recover scatterer properties. Similar efforts use refractive propagation models to recover properties of refractive media [6, 24, 25, 49, 55].

This paper seeks volumetric recovery of a three dimensional (3D) heterogeneous highly scattering medium. Furthermore, this work performs recovery in a very large scale: the atmosphere embedded with clouds. The data comprises images acquired from multiple directions [50], as illustrated in Fig. 1. Such a setup samples the scene’s lightfield [1, 3, 23, 26, 28]. 3D volumetric recovery is achieved in various domains using tomography, finding wide use in biomedical imaging [15, 52] and computational photography [6, 29, 49, 53]. However, this work faces several important challenges. First, due to the large volumes involved, our setup is passive, using the steady, uniform and collimated Sun as the radiation source. This is contrary to most tomography setups, in which the source is controllable. Second, in most tomographic models, as in X-ray, direct-transmission [34] forms the signal, while small-angle scattering has been treated as a perturbation. In contrast, in a medium as a cloud, the source and detector are generally not aligned: scattering including high orders is the dominant signal component.
Previous works on scattering tomography focus on limits of the scattering order: either diffusion [9, 21] or single-scattering [2]. However, scattering objects, as clouds, are complex: they can exhibit diffusion in their core, low-order scattering in their boundaries and interaction with their surrounding. To avoid reliance on such scattering order approximations, we use the 3D radiative transfer equation (RTE) as the image formation model. However, avoiding such scattering approximations significantly complicates the model, jeopardizing the prospects of its inversion. To make any type of tomography a practical tool, the inverse problem must be tractable. It is thus necessary to find means to efficiently invert the model, as this paper derives.

The derived mathematical multi-scatter heterogeneous model and algorithm principles can be applied to various media. This paper makes further focus on clouds, which are scattering media made of suspended water droplets. Clouds reflect much of the Sun’s radiation out to space, while trapping emitted terrestrial radiation. Clouds thus play a major role in the Earth’s radiation budget and the understanding of climate evolution [44], yet their influence over climate change still has a large uncertainty [11]. There is thus motivation to sense clouds in detail.

Lidars and in-situ sampling provide local small-scale data. Current optical remote sensing of Earth’s atmosphere generally does not yield 3D volumetric mapping. Rather, remote sensing methodology has largely assumed a plane-parallel atmospheric geometry, with horizontally uniform properties. This crude geometry limits recovery to simple parameters [36, 37, 42]. Moreover, this approximation of atmospheric structure causes biases of the retrieved parameters in most cases [14]. Our 3D volumetric recovery avoids the plane-parallel assumption. The method is demonstrated on images captured from a high altitude aircraft. It is also validated using established atmospheric models coupling fluid dynamics and cloud micro-physics.

2. Theoretical background

2.1. Image Formation Model: Radiative Transfer

Our image formation (forward) model is steady-state 3D radiative transfer. A domain $\Omega \subset \mathbb{R}^3$ has boundary $\partial \Omega$, whose outward facing normal is $\vartheta$ (Fig. 1). At position $x \in \Omega$ and direction of propagation $\omega \in \mathbb{S}^2$ (unit sphere), the radiation field is $I(x, \omega)$. Dependency on wavelength $\lambda$ is omitted, to simplify the explanation. Let $\omega \cdot \vartheta < 0$ define incoming radiation. The boundary condition is

$$I(x, \omega) \triangleq I_{BC}(x, \omega) \quad \text{when} \quad \omega \cdot \vartheta < 0, \quad x \in \partial \Omega. \quad (1)$$

Radiative transfer satisfies [10]:

$$\omega \cdot \nabla I(x, \omega) = \beta(x) [J(x, \omega) - I(x, \omega)] \quad x \in \Omega, \quad (2)$$

where $\beta$ is the $x$-dependent extinction coefficient, while

$$J(x, \omega) = \frac{c_0}{4\pi} \int_{\mathbb{S}^2} p(x, \omega \cdot \omega') I(x, \omega') d\omega'$$

is the source function (in-scattering term) [10], neglecting visible light emission by the medium. Here $c_0$ is the single scattering albedo and $p(x, \omega \cdot \omega')$ is the phase function at $x$. The phase function describes the fraction of energy scattered from $\omega'$ to $\omega$ by an infinitesimal volume. Equations (1–3) define a complete radiative transfer forward model for an externally illuminated, non-emitting medium.

Integrating Eq. (2) along a specific direction $\omega$ results in an integral form of the 3D RTE [10, 31]

$$I(x, \omega) = I_{BC}(x_0, \omega) \exp \left[ - \int_{x_0}^x \beta(r) dr \right]$$

$$+ \int_x^x J(x', \omega) \beta(x') \exp \left[ - \int_x^{x'} \beta(r) dr \right] dx'. \quad (4)$$

Here $x_0$ is a point on the boundary (see Fig. 1). Equation (4) accumulates scattered radiance along a line of sight, weighted by the corresponding extinction. By $\int_x^{x'} f(r) dr$, we mean a line integral over a field $f(x)$ along the segment extending from $x$ to $x'$. Numerically, this is preformed by back-projecting a ray through the medium.

Equations (3,4) express a recursive interplay of the fields $J$ and $I$, as illustrated in Fig. 2. A recursion effectively amounts to a successive order of scattering, or a Picard iteration [18]. Had $J(x, \omega)$ been computed only through incoming solar radiation, without recursion, the result would have been a single scattering approximation.

2.2. Spherical Harmonics Discrete Ordinates

Numerically solving the radiative transfer is a balance between speed and accuracy. Monte Carlo (MC) methods can handle very complex media, including sharp changes in optical parameters. This makes MC particularly accurate in rendering of surfaces. In MC, radiometric quantities are attained by random sampling the infinite domain of possible light paths. This computational process is very slow, particularly for multi-view images. Faster rendering using less random samples increases noise.
Deterministic RTE solvers discretize the spatial and angular domain. Discretization biases \( I(x, \omega) \) towards smooth solutions. Nevertheless, volumetric clouds are smoother than surfaces, thus a computed smooth \( I(x, \omega) \) is consistent with the nature of cloud fields. Deterministic solvers are thus prime tools in atmospheric rendering. Moreover, when seeking many radiometric outputs of the same scene, e.g. in multiple viewpoints, a model that solves the RTE directly has favorable computational cost.

A very efficient, deterministic solver is the spherical harmonic discrete ordinates method (SHDOM) \([18, 31]\), which relies on two principles. (i) A spherical harmonics representation for the scatter field allows for efficient computation of angular integrals. (ii) Discrete ordinates models radiation flow along specific directions within the domain. Ref. \([41]\) compares atmospheric MC and SHDOM.

### 2.3. Air and Cloud Water Droplets

For air molecules and cloud water droplets, \( \alpha \approx 1 \) in visible light. Molecules follow the Rayleigh scattering law, which uniquely determines the spatially invariant molecular phase function \( \rho_R(\omega : \omega') \). The Rayleigh scattering coefficient \( \beta_R \) is analytically known per air density. Air density varies mainly with altitude \( z \). With localized tornadoes as exception, air density varies slowly in space and time, and mapped over Earth using long established systems.

The change of refractive index between air and cloud water droplets creates scattering, represented by a cloud scattering coefficient \( \beta_c(x) \) and phase function \( p_c(\omega : \omega') \). The total extinction and phase function are respectively
\[
\beta(x) = \beta_c(x) + \beta_R(z) \tag{5}
\]
\[
p(x, \omega : \omega') = p_c(\omega : \omega') \beta_c(x) + \rho_R(\omega : \omega') \beta_R(z). \tag{6}
\]

The function \( p_c \) is determined through Mie theory by the droplet size distribution. The size varies mainly vertically, within typical air masses. Vertical variations follow curves, whose parameters are measured from satellites \([45]\). 3D variations are thus mainly attributed here to \( \beta_c(x) \).

### 3. Tomographic Recovery - Inverse Model

We seek to recover \( \beta(x) \) within the volume of a cloud. This is equivalent to seeking \( \beta_c(x) \), since \( \beta_R(z) \) is known. The recovery is based on images, with a complex image formation model. An efficient approach must be derived for such a complex recovery to be contemplated. Note that Eq. (4) depends on \( \beta(x) \) in two ways. One dependency on \( \beta \) is explicit, through line integrals over straight back-projected rays, that are easy to compute. The other dependency is implicit, through \( J \). The implicit dependency is complicated and non-local: a change in \( \beta(x_1) \) can cause a change in \( J(x_2) \). However, for a given, fixed \( J \), it is easy to compute, through (4), the radiance \( I \) and \( \partial^2 I/\partial^2 \beta \). This observation provides a key for computationally realistic tomographic recovery, which is now explained.

#### 3.1. Operator Notation

Following \([5, 7]\), we use operator notations. For a given boundary condition, the radiance forward mapping \( I(x, \omega) = I(\beta) \) is an operator that transforms an extinction field \( \beta \) into a radiance field \( I \). Let us decompose this mapping into two operators, \( I(\beta) = T(\beta) J(\beta) \). Here \( J(x, \omega) = J(\beta) \) is the in-scatter forward mapping from a field \( \beta \) to a field \( J \). The operation \( T(\beta) \) transforms an in-scatter field \( J \) to a measurable radiance field by the simple line integrals of Eq. (4).

An aperture function \( w \in \Omega \times \mathbb{S}^2 \), defines collection of radiance by a detector, over a spatial and angular support. Measurements are thus an operator
\[
\mathcal{M}_w I(\beta) = \langle w, I \rangle_\Omega, \quad \text{where } \langle \cdot, \cdot \rangle_\Omega = \int \int \int d\omega dx. \tag{7}
\]

For an idealized single-pixel detector positioned at \( x^* \), collecting radiation flowing in direction \( \omega^* \),
\[
\mathcal{M}_w I = \langle \delta(x - x^*) \delta(\omega - \omega^*), I \rangle_\Omega = I(x^*, \omega^*). \tag{8}
\]

Consequently, the forward model is
\[
\mathcal{F}_w (\beta) = \mathcal{M}_w I(\beta) = \mathcal{M}_w T(\beta) J(\beta). \tag{9}
\]

For numerical recovery, the sought field is discretized
\[
\beta(x) = \sum_{k=1}^{N_{\text{grid}}} \beta_k b_k(x), \tag{10}
\]
where \( \{\beta_k\}_{k=1}^{N_{\text{grid}}} \) are discrete parameters, \( b_k(x) \) is a unitless interpolation kernel and \( N_{\text{grid}} \) is the number of grid points. Let \( y \) be a measurement vector and \( (\cdot)^T \) denote transposition. Tomographic reconstruction is an estimation of \( \beta = (\beta_1, \ldots, \beta_{N_{\text{grid}}})^T \), that minimizes a data fit cost
\[
\beta = \arg \min_{\beta} \mathcal{E}[y, \mathcal{F}(\beta)]. \tag{11}
\]

Solving the minimization problem utilizes the gradient of \( \mathcal{E} \) with respect to \( \beta \). In Eq. (5), \( \beta_R(z) \) is known, thus \( d\mathcal{E}/d\beta \) = \( d\mathcal{E}/d\beta_c \). The gradient is traditionally estimated iteratively, which would require \( O(N_{\text{grid}}) \) simulations of the forward model, per iteration. The complexity is exacerbated by the complicated and non-linear form of the forward operator \( \mathcal{F} \). Differentiation using an adjoint RTE was theorized in \([32]\). A theory and initial results of inverse rendering using \( P_n \) approximation are shown in \([54]\).
works that do not attempt 3D volumetric recovery, stochastic gradients [22] are used in a homogeneous medium, while numerical differentiation estimates unidirectional path integrals [13, 30]. Despite seeking non-volumetric recoveries, these works report prohibitive computational complexity.

### 3.2. Scalable Approach

To turn the hypothetical (11) to a feasible, tractable method, we simplify [27] the computations. Instead of optimizing a function whose gradient is complex to compute, we efficiently optimize \( \beta \) using surrogate functions that evolve through iterations (Fig. 3). Let \( \beta_n \) be an estimate of \( \beta \) in iteration \( n \). The first step computes the in-scatter field, which corresponds to the current estimate \( \beta_n \)

\[
J_n = \mathcal{J}(\beta_n).
\]

(12)

This is the computationally complex part, hence we do not estimate its gradient. In fact, we hold \( J_n \) constant for a while, despite evolution of \( \beta \). Let \( \mathcal{F}(\beta;J_n) = \mathcal{MT}(\beta) J_n \) serve as a surrogate function in which \( J_n \) is fixed. In the second step, keeping \( J_n \) fixed, the following optimization finds the next estimate of \( \beta \)

\[
\beta_{n+1} = \arg \min_{\beta} \mathcal{E}[y, \mathcal{F}(\beta; J_n)].
\]

(13)

Data-fit using weighted least squares has the form

\[
\mathcal{E}[y, \mathcal{F}(\beta; J_n)] = \frac{1}{2} \left[ y - \mathcal{MT}(\beta) J_n \right]^T \Sigma_{\text{meas}}^{-1} \left[ y - \mathcal{MT}(\beta) J_n \right].
\]

(14)

Here \( \Sigma_{\text{meas}} \) is the covariance matrix of the (uncorrelated) measurements. The variance of measurement \( w \) is \( \sigma_w^2 \).

Given measurement vector \( y \) of length \( N_{\text{meas}} \) and \( J_n \), solving (13,14) is simple using gradient-based methods.

\[
\frac{\partial}{\partial \beta} \mathcal{E}[y, \mathcal{F}(\beta; J_n)] = \sum_{w=1}^{N_{\text{meas}}} \frac{1}{\sigma_w^2} \left[ F_w(\beta; J_n) - y_w \right] \mathcal{M}_w \left[ \frac{\partial}{\partial \beta} \mathcal{T}(\beta) \right] J_n.
\]

(15)

For a detector defined in (8),

\[
\mathcal{M}_w \left[ \frac{\partial}{\partial \beta} \mathcal{T}(\beta) \right] J_n = A_{w,k} + B_{w,k},
\]

(16)

where

\[
A_{w,k} = c_k(x_0) I_{BC}(x_0, \omega^*) \exp \left[ - \int_{x^*}^{x_0} \beta(r) \, dr \right],
\]

\[
B_{w,k} = \int_{x^*}^{x_0} J_n(x, \omega^*) \left[ b_k(x) + c_k(x) \beta(x) \right] \exp \left[ - \int_{x^*}^{x} \beta(r) \, dr \right] \, dx.
\]

(17)

The factor \( c_k(x) = - \int_{x^*}^{x} b_k(r) \, dr \) can be pre-computed, as it does not depend on the sought field. Given the gradient (15), Eq. (13) can be solved using gradient descent

\[
\beta_{n+1} = \beta_n - \Delta \frac{\partial}{\partial \beta} \mathcal{E}[y, \mathcal{F}(\beta; J_n)],
\]

(18)

where \( t \) indexes a gradient-descent step, and \( \Delta \) is the step size. After every \( N_\beta \) gradient descent steps, the field \( J \) is updated using SHDOM. Then, gradient-descent is resumed, using the updated \( J \), for another set of \( N_\beta \) gradient descents, and so on. Starting with an initial guess \( \beta_0 \), Eqs. (12,13,18) define an iterative optimization process. Eqs. (12,13) are alternated repeatedly until convergence.

In optimization problems, particularly nonlinear ones, the step size \( \Delta \) needs to be well set. As a preliminary rule of thumb, we found that for stability, \( \Delta \) needs to be lower, when the effective optical depth (not a 3D function) of a cloud is lower. Optical depth is currently retrievable using 1D radiative transfer methods [36].

### 3.3. Computational Efficiency

The surrogate function enables a major reduction in computational complexity, enabling for the first time, feasible 3D recovery. The most expensive part of the process is 3D rendering including multiple scattering, expressed by \( \mathcal{J} \). Hence, \( \mathcal{J} \) must be performed sparingly. Let there be \( N_{\text{DOF}} \) degrees of freedom (unknowns) to recover. In the pioneering work of Ref. [22], focusing on retrieval of a homogeneous anisotropic medium, each gradient descent operation requires \( \mathcal{O}(N_{\text{DOF}}) \) operations of \( \mathcal{J} \) (rendering operator).

In our optimization of \( \beta \), a gradient descent of the surrogate function uses a fixed \( J_n \), hence no operation of \( \mathcal{J} \) is made, irrespective of \( N_{\text{DOF}} = N_{\text{grid}} \). The operator \( \mathcal{J} \) is applied sporadically over time, with frequency that is unrelated to \( N_{\text{grid}} \). Hence, our approach accelerates the most expensive part of gradient descent by \( \mathcal{O}(N_{\text{grid}}) \), facilitating optimization of \( \mathcal{O}(10^5) \) unknowns in a short time. Our method is thus scalable.
reflectance is affected by a 10 m/s wind and a typical 3D grid. The clouds here hover above open ocean, whose key output of the LES is liquid water content over a controlled scene, we use a large eddy simulation (LES) to generate a cloud field (Fig. 4). The large eddy simulation (LES) is a comprehensive tool used by atmospheric scientists to computationally-create physically correct clouds [50]. The key output of the LES is liquid water content over a 3D grid. The clouds here hover above open ocean, whose reflectance [51] is affected by a 10 m/s wind and a typical chlorophyll concentration of 0.01 mg/m³ [40]. Here are additional scene parameters.

### Atmospheric Constituents:
The droplet size is Gamma-distributed, with effective droplet radius \( r_{\text{eff}} = 10 \mu \text{m} \) effective variance \( v_{\text{eff}} = 0.1 \), which are typical values [43]. Mie scattering theory converts these quantities into \( \beta_c(x) \) and \( p_c(\omega' \cdot \omega') \), the cloud phase function. We model molecular scattering using a summer mid-latitude vertical distribution [4], at altitudes ranging within \( z \in [0, 20] \) km. We use \( \lambda = 672 \) nm, where Rayleigh total optical thickness [16, 17] of non-cloudy air is only \( \sim 0.05 \).

### Image Rendering:
The top of the atmosphere is irradiated by collimated sunlight, directed as described in Fig. 4. An SHDOM code [18] which is popular in atmospheric 3D radiative transfer, emulates measurements similar to those taken by the Multi-angle Spectro-Polarimeter Imager (AirMSPI) [17] at 20 m resolution. The 9 viewing zenith angles are \( \pm 70.5^\circ, \pm 60^\circ, \pm 45.6^\circ, \pm 26.1^\circ \), and \( 0^\circ \), where \( \pm \) indicates forward/backward along the flight path. Images as viewed from the instrument are rendered in Fig. 4. Poisson and quantization noise are included, according to the specifications of AirMSPI [17].

### 5.2. Recovery Results
We analyzed two atmospheric volumes, marked by green and red boxes in Fig. 4. Their respective dimensions are \( 0.72 \times 0.72 \times 1.44 \text{km}^3 \), \( 1.32 \times 2.22 \times 2.2 \text{km}^3 \). The analysis used \( \Delta = 200 \) and \( N_\beta = 7 \) and open horizontal boundaries, expressing observation of an isolated cloud. Updates of the surrogate function stopped when the cost function declines to 1% of its initial value. MATLAB was used on a 2.50 GHz Intel Xeon CPU. The rendering step, implemented in FORTRAN, was parallelized on 8 cores.

The converged reconstructions are displayed in Figs. 5,6 along with the ground-truth and a 3D relative error map. We quantify the recovery error using two measures defined in [2]. For the cloud marked in green (Fig. 4), the relative error in overall recovered mass is \( \delta = (5 \pm 0.1)\% \). The relative local error is \( \epsilon = (33 \pm 2)\% \). Fig. 7 displays \( \epsilon \) in three slices. The error is larger at more opaque regions within the cloud. A scatter plot of true vs. estimated values is shown in Fig. 7c: its correlation is \( \rho = 0.94 \). For the cloud marked in red (Fig. 4), \( \delta = 30\%, \epsilon = 70\% \), due to the loss of signal. Here \( \rho = 0.76 \). These results evolve from an initialization of no-cloud, with neither priors nor regularization on cloud structure. Runtime analysis is displayed in Fig. 8.

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1In [33], Fig. 4 is originally rendered using MC.
Figure 5. The unknown extinction field is discretized to a $36 \times 36 \times 36$ grid (46,656 unknowns). A volumetric comparison between the true LES-generated cloud and the recovered cloud, based on initialization that assumed no cloud at all. It is evident from the relative error map that the error is larger in the more opaque regions of the cloud.

Figure 6. The unknown extinction field is discretized to a $66 \times 111 \times 43$ grid (315,018 unknowns). A volumetric comparison between the true LES-generated cloud and the recovered cloud, based on initialization that assumed no cloud at all. The cloud is extremely optically thick here, completely dissipating the signal (down to sensor noise level) in some areas.

6. Large-Scale Field Experiment

6.1. Real Data and Its Pre-Processing

It is desirable to apply this approach to real data, captured in the huge outdoor field, from multiple remote views [50]. In 2010 NASA initiated field campaigns with AirMSPI [17] at 20 km altitude, aboard NASA’s ER-2 aircraft. AirMSPI has an eight-band push-broom camera, mounted on a gimbal for multi-angular observations over a $\pm 67^\circ$ along-track range. AirMSPI had undergone extensive geometric and radiometric calibration, to enable highly accurate quantitative measurements and subsequent products. In a step-and-stare mode, the spatial resolution is 10m.

We use the 660nm channel of data from a Pacific flight\(^2\) done Feb/6/2013 at 20:27 GMT, around global coordinates 32N 123W. The flight path and three out of the nine view angles are displayed in Fig. 9a. We examine an atmospheric portion of $2.6 \text{ km} \times 3.4 \text{ km} \times 2.4 \text{ km}$ in East-North-Up coordinates.

Clouds move due to wind at their altitude, while AirMSPI flies. Motion along-track is difficult to resolve by images, since it aliases as parallax, globally affecting altitude estimation. Motion across track was estimated by aligning consecutive frames. This method yielded an assessed cross-track motion of $\approx 37 \text{ km/h}$.

\(^2\)https://eosweb.larc.nasa.gov/project/airmspi
6.2. Results

The assumed open ocean parameters we used are chlorophyll concentration of 0.01 mg/m³ and surface wind of 15 km/h. The boundary conditions, droplet size distribution, update scheme and convergence criteria are as described in Sec. 5, while here $\Delta = 10$. The extinction field is discretized to $43 \times 56 \times 35$ grid points (86,688 unknowns). Based on the nine views, the converged volumetric reconstruction is displayed in Fig. 9d. The extinction values recovered by our reconstruction indicate an optical mean-free-path of 100-300 meters inside this cloud.

For cross-validation of the method, we excluded the nadir image data from the recovery process, thus using only eight out of the nine raw views in the 3D recovery. Afterwards, we used the recovered cloud to render the missing nadir view. Figure 9b,c compares the raw AirMSPI nadir image to the rendered corresponding view. The same cross-validation process was repeated for the $+47^\circ$ view angle (Fig. 9e,f). The coarseness of the estimated images is due to the cloud-voxel resolution (60m $\times$ 60m $\times$ 70m), which is lower than the AirMSPI sampling resolution (10m $\times$ 10m). Some of the artifacts evident in the volumetric reconstruction are due to the ocean, whose true parameters were not calibrated by us.

7. Summary

This work derives a framework for 3D tomography in scattering media, and in a large uncontrolled environment, where clouds reside. In this type of tomography, the signal is dominated by multiply scattered radiance and the source may be uncontrolled. Neither small angle nor an approximate scattering order limit are assumed by our work. To solve the problem in a tractable way, we develop a surrogate function suitable for the image formation model. This approach aims to enable large-scale tomography of the particulate atmosphere, and thus advance our understanding of the physical processes involved. It can also find use in biomedical tomography, away from the small-angle, single-scattering or diffusion limits.

In computer vision, many recent studies attempt dehazing, i.e., background scene recovery through a scattering medium. The dominant model used so far in dehazing under natural lighting has been based on a single-scattering approximation, ignoring higher-order scattering. Our work herein suggests that an inverse problem including an arbitrary order of atmospheric daylight scattering is solvable. Hence, dehazing may benefit from methods presented here.

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Figure 9. (a) Google Maps illustration of AirMSPI push-broom scan over the Pacific. A domain is viewed at nine angles (three displayed above). (b) Raw AirMSPI measurement at nadir view. (c) Nadir rendered view of a 3D cloud estimated using data that had excluded the nadir. (d) Recovered volumetric extinction field at +47° view. (e) Raw AirMSPI measurement at +47° view. (f) The +47° rendered view of a 3D cloud estimated using data that had excluded the +47° raw view.

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