

On the phase of natural stochastic structured textures and its
application in deconvolution and image decomposition

Ido Zachevsky and Yehoshua Y. Zeevi

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