## ELECTRONS ACCELERATION in an INVERTED MEDIUM

#### Levi Schächter



Technion - Israel Institute of Technology Department of Electrical Engineering



- Overview and Motivation
- Particle Acceleration in Inverted Medium
- Wake Amplification and Acceleration
- Parameter Analysis
- Experimental Setup
- Summary



## Laser & Plasma

Laser Wake-Field
Plasma Beat-Wave

E-beam & Plasma Wake-Field Acc.

Laser & Inverse of **Radiation Processes** M Inverse Cerenkov M Inverse FEL Juverse Smith-Purcell E-beam & Structure Two-Beam Acc. Cerenkov Wake-Field



Intense and short laser pulse

Two medium power laser pulses

 $\omega_1 - \omega_2 = \omega_p$ 

Laser & Plasma

Laser Wake-Field

M Plasma Beat-Wave





Driving bunch

Test bunch

Space-charge wave



**Inverse FEL** 

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**Inverse Cerenkov** 

Laser & Inverse of **Radiation Processes** Inverse Cerenkov M Inverse FEL Juverse Smith-Purcell  $\hat{\mathbf{I}}$ Ţ

**Inverse Smith-Purcell** 

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#### **Two-beam** Accelerator



#### Cerenkov Wake-Field Accelerator



Phase velocity = velocity of driving bunch



Laser & Plasma

🥙 Plasma Beat-Wave

Inverse Laser ?

Laser & Inverse of Radiation Processes

Inverse Cerenkov
Inverse FEL
Inverse Smith-Purcell

E-beam & Plasma Wake-Field Acc.

Amplify a Wake ? Amplify Cerenkov Radiation ? E-beam & Structure

Two-Beam Acc. Cerenkov Wake-Field

### **Particle Acceleration by Inverted Medium**

**Passive Dielectric** 

Cerenkov Radiation
 Decelerating Force





Inverted Medium

> Negative Resistivity

Induced Currents

Accelerating Force

Phys. Lett. A, 205, p.355 (1995)

PRE, 53, p.6427 (1996).

#### **Particle Acceleration by Active Medium**





Laser & Plasma

🔥 Laser Wake-Field

🥙 Plasma Beat-Wave

Laser & Inverse of **Radiation Processes** 

Inverse Cerenkov 💽 Inverse Laser

M Inverse FEL Merse Smith-Purcell

E-beam & Plasma Wake-Field Acc.

Amplify a

Wake?

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Amplify Cerenkov Radiation ? E-beam & Structure

Two-Beam Acc. Cerenkov Wake-Field



The dispersion equation:

$$D(\omega) \equiv J_0 \left(\frac{\omega}{c} R \sqrt{\epsilon - \beta^{-2}}\right) + \frac{1}{\gamma \beta} \frac{\epsilon}{\sqrt{\epsilon - \beta^{-2}}} J_1 \left(\frac{\omega}{c} R \sqrt{\epsilon - \beta^{-2}}\right)$$

 $K_0\left(\frac{\omega}{c}\frac{R}{\gamma\beta}\right)$ 

 $\frac{1}{K_1\left(\frac{\omega}{c}\frac{R}{\gamma\beta}\right)}$ 

*Inversion*:  $\omega_p^2 < 0$ 

For relativistic particles ( $\gamma >>1$ ) the poles are determined by

Ignore resonance

$$D(\omega) \cong J_0\left(\frac{\omega}{c}R\sqrt{\varepsilon(\omega)-1}\right) = 0 \implies \frac{\omega_0}{c}R\sqrt{\varepsilon_r-1} = p$$

Resonance introduces a change:

$$\omega = \omega_0 + \delta \omega \implies \delta \omega = \pm j \frac{|\omega_p|}{2\sqrt{\varepsilon_r} - 1}$$

#### Wake-Field Amplification - Dispersion Curves



Although multiple modes are possible in this geometry only a single mode will be amplified - provided the mode separation is sufficient.

#### Wake-Field Amplification - Gradient

Length of the driving bunch

Longitudinal component of the electric field:

$$E_{z}(\mathbf{r}, z, t) \cong E_{d} J_{0}\left(p\frac{r}{R}\right) \sin[\omega_{0}(t - z/v)]e^{\left|\delta\omega\right|(t - z/v)}$$
Charge of the trigger bunch
$$\left[\left(R_{d}\right)\right]\left[\cdot\left(\omega_{0}\Delta^{\prime}\right)\right]$$

$$E_{d} \cong \frac{q}{4\pi\epsilon_{0}\epsilon_{r}R^{2}J_{1}^{2}(p)}$$

$$\begin{array}{c}
 J_1\left(p\frac{Rd}{R}\right) \\
 0.5 p\frac{Rd}{R} \\
 \hline
 \end{array}
 \end{array}
 \begin{bmatrix}
 \sin\left(\frac{\omega_0}{v}\frac{\Delta}{2}\right) \\
 \frac{\omega_0}{v}\frac{\Delta}{2} \\
 \hline
 \end{array}$$

Radius of the driving bunch

Total power flow

Interaction Impedance

$$Z_{\text{int}} \equiv \frac{(E_z R)^2}{2P} = \sqrt{\frac{\mu_0}{\epsilon_0} \frac{\epsilon_r - 1}{\pi J_1^2(p)}} \propto \frac{\omega_0}{c} R$$

Zero of Bessel function

### Wake-Field Amplification - Saturation

At high intensities the inversion is reduced by the field:

$$\delta \omega \rightarrow \delta \omega \frac{1}{1 + (E/E_{cr})^2}, \quad E_{cr} \equiv \frac{\hbar}{\mu \sqrt{\tau T_2}}$$
  
Dipole moment

Relaxation time constants

Consequently, at a distance d after the driving bunch

$$E = E_d \exp\left\{\frac{d}{c} |\delta\omega| \frac{1}{1 + (E/E_{cr})^2}\right\}$$

and for a given accelerating gradient  $(E_{acc})$  the witness bunch

$$d_{w} = \frac{c}{|\delta\omega|} \left[ 1 + \left(\frac{E_{acc}}{E_{cr}}\right)^{2} \right] \ln\left(\frac{E_{acc}}{E_{d}}\right)$$

### Wake-Field Amplification - Parameter Analysis

Geometric and Electrical parameters

R[cm] = 1D[cm] = 100 $R_d [cm] = 0.01$  $\Delta [cm] = 0.1$  $E_{acc} [GV/m] = 1$  $E_{sat} [MV/m] = 10$ 

### Wake-Field Amplification - Parameter Analysis

	ND:YAG	TI SAPPHIRE
	$[Y_3 \overline{A}_{L5} \overline{O}_{12}]$	$[TI^{3+}: AL_2O_3]$
ε <sub>r</sub>	1.82	1.76
λ [μm]	1.06	0.514
N <sub>dop</sub> [atom/cm <sup>3</sup> ]	5.8x10 <sup>19</sup>	3.3x10 <sup>19</sup>
Dopant	Yttrium (1%)	Ti <sub>2</sub> O <sub>3</sub> (0.1%)
p	$5.362 \times 10^4$	9.981x 10 <sup>4</sup>
$Z_{int}$ [M $\Omega$ ]	8.64	16.41
Energy [kJ]	3.24	3.8
N <sub>acc</sub> [50% eff]	$1.0 \times 10^{13}$	$1.2 \times 10^{13}$
$\delta\omega/\omega_0$	0.134	0.051
$E_d [V/m]$	3x10 <sup>-4</sup>	6x10 <sup>-5</sup>
$d_w[m]$	0.36	0.49
P[MW]	5.78	3.05
S[MW/cm <sup>2</sup> ]	1.8	0.97
Gain [dB/cm]	6.9	5.4



• PASER: Electrons gain energy stored in the medium. For ``competitive`` gradients the charge density required is very high thus the alternative is

- Wake-Field Amplification. Energy is in the medium -- no need for optical system.
- Acc. mode moves at the speed of trigger bunch.
- Inherent longitudinal electric field.
- Growth controlled by the population inversion.
- Less than  $0.1\pi$  mm-mrad emittance growth.



• Vacuum acc. by combining solid-state medium.

• Although the transverse dimension entails many modes excitation, they all move at  $V_d$  and all oscillate at the frequency of the medium  $\omega_0$ 

 Nd: YAG and Ti: Sapphire store sufficient energy to accelerate more than 10<sup>9</sup> electrons ignoring the longitudinal space-charge effect.

# **Experiment Suggested at ORION** • Goal: Acc. with Energy Stored in the Medium **Amplification of Cerenkov Radiation** $\epsilon(\omega)$ Investigate: Saturation effects Energy out vs. Energy stored Trigger bunch effect ( $N_{d}$ , $\gamma_{d}$ , energy spread) Transition radiation effect.